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Fifth Semester B.E. Degree Examination, May/June 2010

Digital Signal Processing

Time: 3 hrs.

Max. Marks:100

Note: 1. Answer any FIVE full questions.
2. Use of Butterworth and Chebyshev tables are not permitted.

- 1 a. Determine the following:
 - i) N pt DFT of $x[n] = W_N^{-mn}$ (05 Marks)
 - ii) 4 pt DFT of $x[n] = \cos\left(\frac{n\pi}{4}\right)$ (05 Marks)
 - iii) DFT of $x[n] = \delta[n]$. (02 Marks)
- b. Determine the 8 point DFT of the sequence $x[n] = [1, 1, 1, 1]$ and plot the magnitude and phase angle spectra. (08 Marks)

- 2 a. Consider the finite length sequence $x[n] = \delta[n] + 2\delta[n-5]$.
 - i) Find the 10 point DFT $X(K)$
 - ii) Find the sequence $y[n]$ that has a DFT given by $Y(K) = e^{j\frac{4\pi}{10}k} X(K)$. (08 Marks)
- b. Let $x[n] = 2\delta[n] + \delta[n-1] + \delta[n-3]$. If $X(K)$ is the 5 point DFT of $x[n]$ and if $Y(K) = X^2(K)$, find IDFT of $Y(K)$. (08 Marks)
- c. Prove the time shifting property of DFT. (04 Marks)

- 3 a. Find the 4 point DFTs of the following sequences, using a single 4 point DFT
 - $x_1[n] = [1, 2, 0, 1]$ and $x_2[n] = [2, 2, 1, 1]$. (10 Marks)
- b. The sequence $x[n] = [1, 2, 3, 3, 2, 1, -1, -2, -3, 5, 6, -1, 2, 0, 2, 1]$ is filtered through a filter whose impulse response is $h[n] = [3, 2, 1, 1]$. Compute the output of the filter $y[n]$ using overlap and save method. Use 9 point circular convolution. (10 Marks)

- 4 a. If $x_1[n] = [1, 2, 0, 1]$ and $x_2[n] = [1, 3, 3, 1]$, obtain $x_1[n] \otimes x_2[n]$ using DIT – FFT algorithm. (12 Marks)
- b. Develop a DIF – FFT algorithm for decomposing the DFT for $N = 6$. Draw the flow diagram. (08 Marks)

- 5 a. A system is specified by the relation $y[n] = \frac{1}{2}y[n-1] + \frac{1}{4}y[n-2] + x[n] + x[n-1]$. Realize the system in the following forms:
 - i) Direct form
 - ii) Cascade form and
 - iii) Parallel form. (12 Marks)
- b. Realize the FIR filter whose transfer function is $H(Z) = 1 + \frac{3}{4}z^{-1} + \frac{17}{8}z^{-2} + \frac{3}{4}z^{-3} + z^{-4}$ in
 - i) Direct form and ii) Cascade form. (08 Marks)

- 6 a. Explain bilinear transformation method of digital filter design. (08 Marks)
 b. Obtain the digital filter equivalent of the analog filter shown in Fig.6(b), using
 i) Impulse invariance transformation and
 ii) Bilinear transformation methods.

Assume the sampling frequency $f_s = 2 f_0$, where f_0 is the cutoff frequency of the analog filter shown

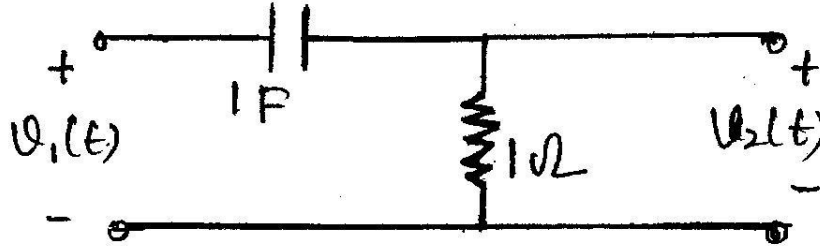


Fig.6(b)

(12 Marks)

- 7 a. Design a digital filter that meets the following specifications:
 $0.8 \leq |H(w)| \leq 1$; $0 \leq w \leq 0.3\pi$
 $|H(w)| \leq 0.2$; $0.6\pi \leq w \leq \pi$

The filter must have a monotonic pass band and stop band frequency response. Use impulse invariance transformation. (14 Marks)

- b. Compare the characteristics of IIR and FIR digital filters. (06 Marks)

- 8 a. Determine the filter coefficient $h_d[n]$ for the desired frequency response of a low pass filter given by,

$$H_d(e^{jw}) = e^{-j2w} \text{ for } -\frac{\pi}{4} \leq w \leq \frac{\pi}{4}$$

$$= 0 \text{ for } \frac{\pi}{4} \leq w \leq \pi$$

If we define the new filter coefficients $h[n] = h_d[n] w[n]$, where
 $w[n] = 1$ for $0 \leq n \leq 4$

$= 0$ otherwise

determine $h[n]$ and also the frequency response $H(e^{jw})$ and compare with $H_d(e^{jw})$. (12 Marks)

- b. Describe in detail, the architecture of general DSP processor. (08 Marks)

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